

Study of Kaon Structure  
using  
 $K_L \rightarrow \pi e \nu e$  and  $K_L \rightarrow \pi e \nu \gamma$   
with external conversion

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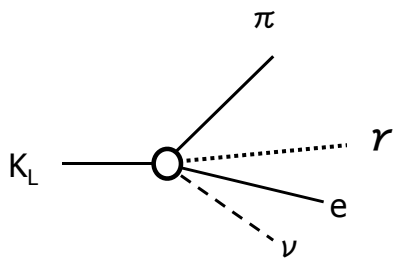
Nemmatsu happyou-kai

# Structure dependent term in radiative Ke3

$p$  :  $\pi^-$   
 $q$  :  $\gamma$   
 $p_\nu$  :  $\bar{\nu}$   
 $p_e$  :  $e^-$

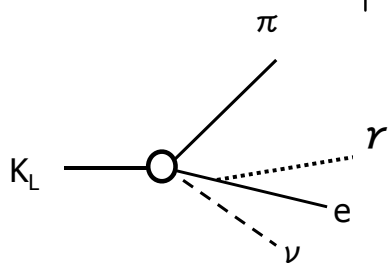
$$T = \frac{G_F}{\sqrt{2}} e V_{us}^* \epsilon^\mu(q)^* \left[ \right.$$

$$\left. \frac{(\hat{V}_{\mu\nu} - A_{\mu\nu}) \bar{u}(p_\nu) \gamma^\nu (1 - \gamma_5) v(p_e)}{\text{Structure dependent}} \right]$$



Structure dependent

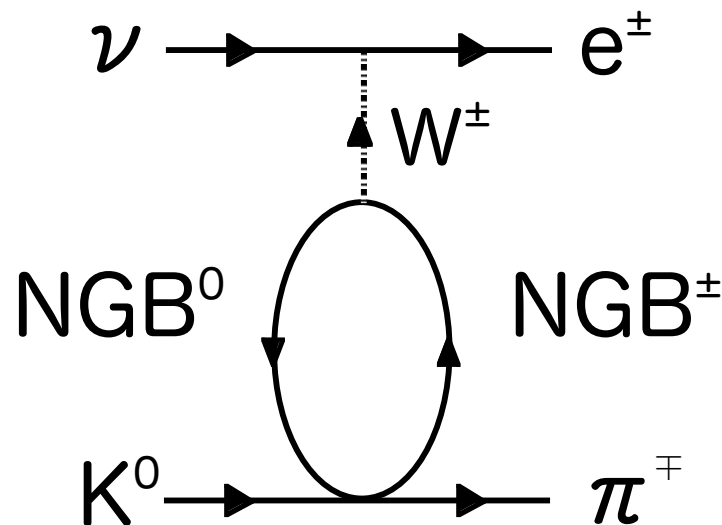
$$+ F_\nu \bar{u}(p_\nu) \gamma^\nu (1 - \gamma_5) \left( \frac{p_\mu}{pq} - \frac{2p_e^\mu + \not{q} \gamma^\mu}{2p_e q} \right) v(p_e) \left. \right]$$



Inner Brem.

$F_\nu$  : Ke3 matrix element  
 $\hat{V}_{\mu\nu}$  : Vector amplitude  
 $A_{\mu\nu}$  : Axial Vector amplitude

# A example to calculate this is Chiral perturbation theory



NGB field of  $u,d,s$  symmetry

$$\begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & -\pi^+ & -K^+ \\ -\pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & -K^0 \\ K^- & -\bar{K}^0 & -\frac{2\eta_8}{\sqrt{6}} \end{pmatrix}$$

In  $\chi$  PT a NGB behaves like a Gauge boson

- In the structure depending case the photon is appended on all charged NGB lines and vertices
- In the inner Brem. case the photon is appended on external lines of electron or pion

# Difficulties

## in the case of radiative $Ke3$

- Structure dependent term in radiative  $Ke3$  is less than 1% of Inner Brem. (theoretical expectation ).
- Measurement of radiative  $Ke3$  is sensitive to accidental photons.



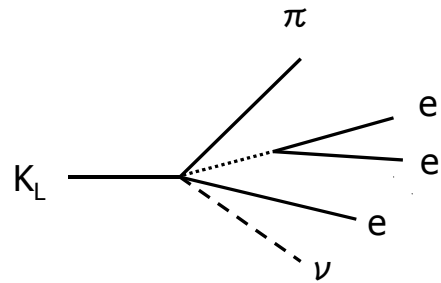
Structure dependent component in  $Ke3\gamma$  has not been observed yet

Experimental  $Br(Ke3\gamma)$  is significantly lower than theoretical predictions as far

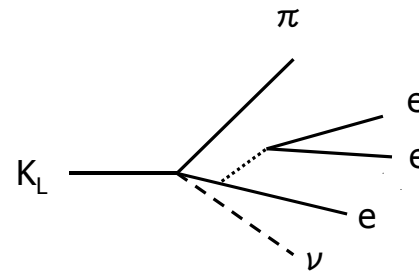
# 1. $K_L \rightarrow \pi e \nu ee$

- $K_L \rightarrow \pi e \nu \gamma^* \rightarrow e^+ e^-$

Structure dependent



Inner Brem.

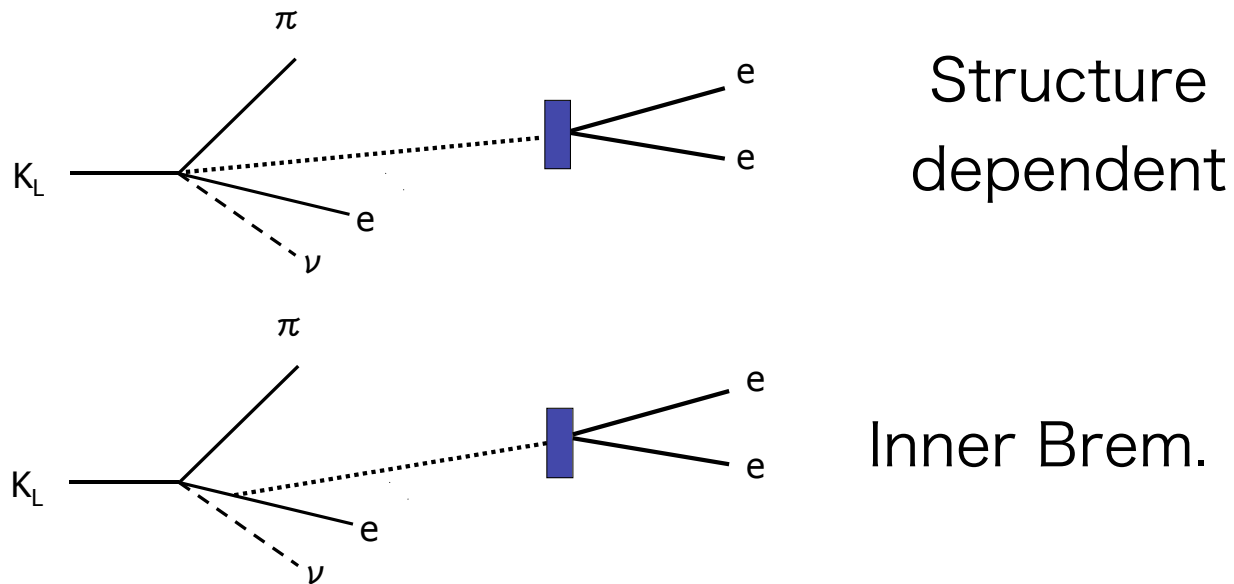


- ?
- 
- A Feynman diagram for an unknown decay  $K_L \rightarrow \pi e \nu \gamma^* \rightarrow e^+ e^-$ . A horizontal line on the left represents the incoming  $K_L$  meson. From its vertex, a solid line goes up and right to a  $\pi$  meson. A dotted line goes right to a vertex where an electron ( $e$ ) and a neutrino ( $\nu$ ) meet. A solid line goes down and right to a vertex where a photon ( $\gamma^*$ ) and another electron ( $e$ ) meet. The  $\gamma^*$  then splits into an electron-positron pair ( $e^+ e^-$ ).

- $K_L \rightarrow \pi e \nu ee$  has not been seen yet.

## 2. External conversion of radiative $K_{e3}$

- External conversion of **real** photon from radiative  $K_{e3}$  can be used to reject accidental photons



$K_L \rightarrow \pi e \nu ee$  and

external conversion of radiative  $Ke3$

	Probe	Inner Brem.	Structure dependent
Virtual photon	$K_L \rightarrow \pi e \nu ee$	?	?
Real photon	Ext. conv. of $Ke3\gamma$	>99%	Direct emission <1%

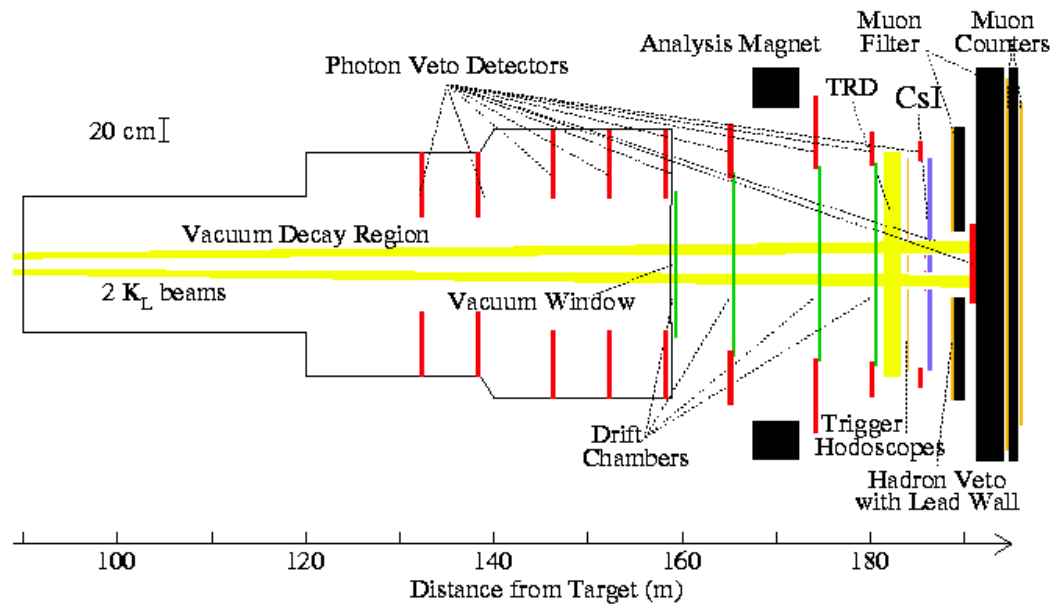
# Experiment

KTeV experiment observed  $2.7 \times 10^{11}$   $K_L$  in '97.

## KTeV Detector, E799 Configuration

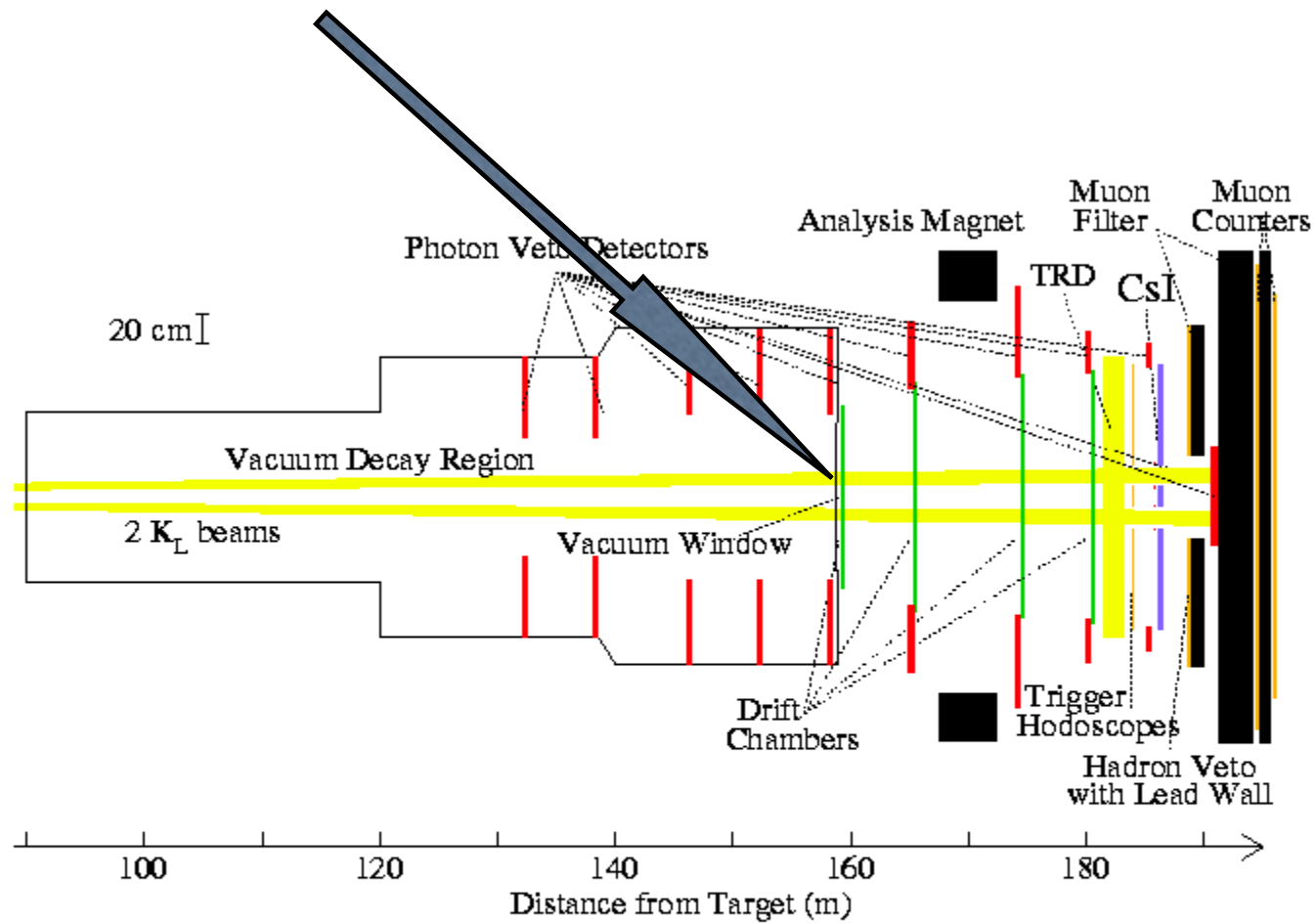
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at  $Z=159\text{m}$ , Vacuum window: 0.0015 radiation length.

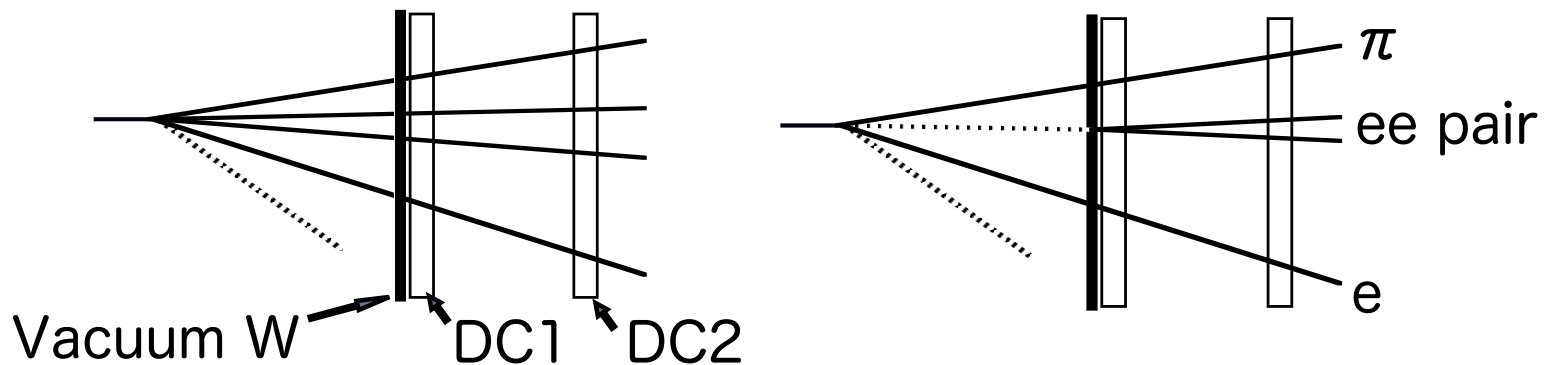


# Event selection

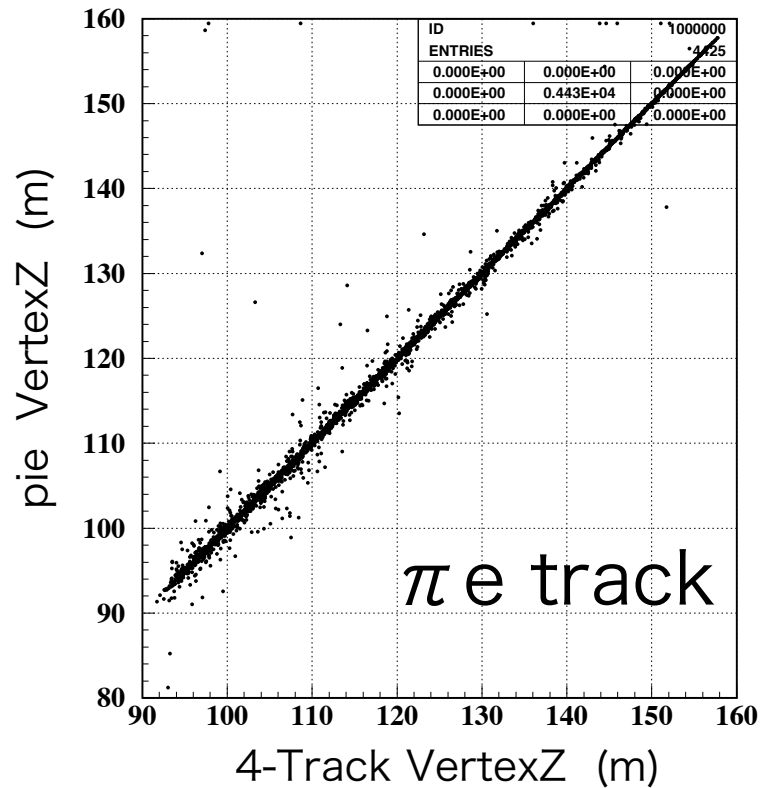
$K_L \rightarrow \pi e \nu ee$	$K_L \rightarrow \pi e \nu \gamma$ with External Conv.
4-Track Event	
4-Track Vtx	2 x 2-Track Vtx
PID- $\pi^{\pm} e^{\mp} e^+ e^-$	PID- $\pi^{\pm} e^{\mp}, e^+ e^-$

# Separation of $K_L \rightarrow \pi e \nu ee$ and $K_L \rightarrow \pi e \nu \gamma$ with External Conv.

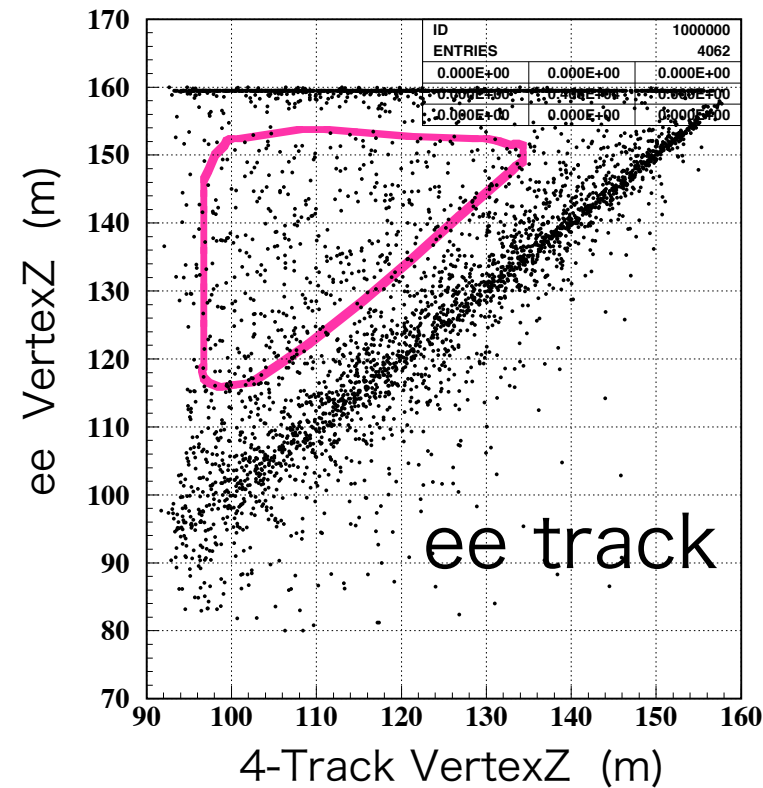
	$K_L \rightarrow \pi e \nu ee$	$K_L \rightarrow \pi e \nu \gamma$ with External Conv.
$\pi e$ -Vtx & $ee$ -Vtx	Agree	some distance
$ee$ -Vtx	not on Vacuum window	on Vacuum window



# $e^+e^-$ vertices of 4-track Vtx candidates stream downward!

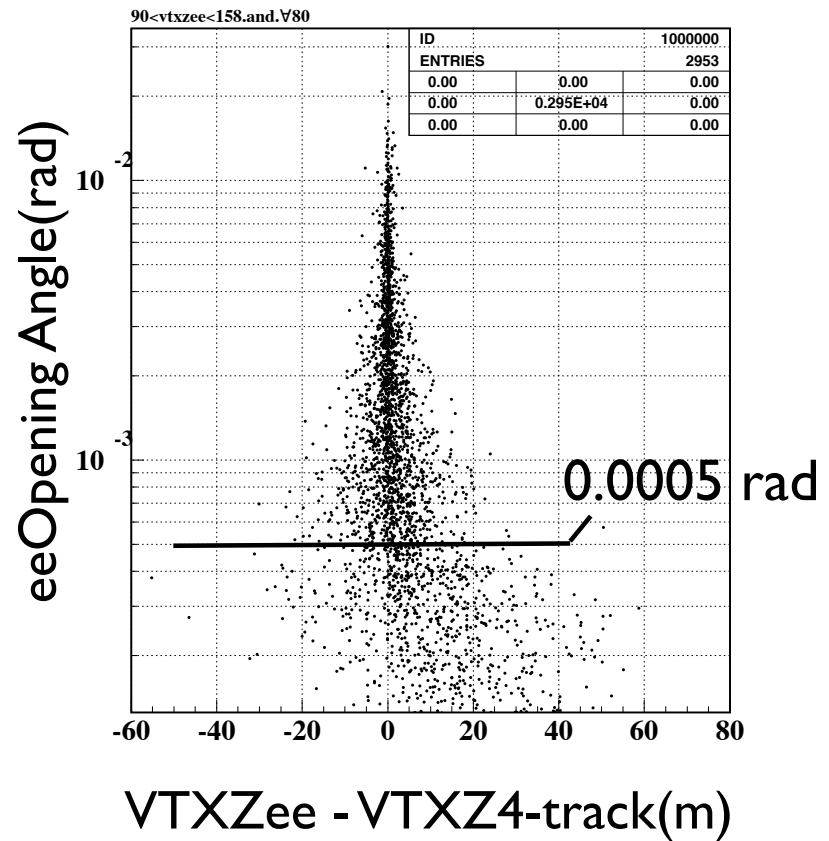
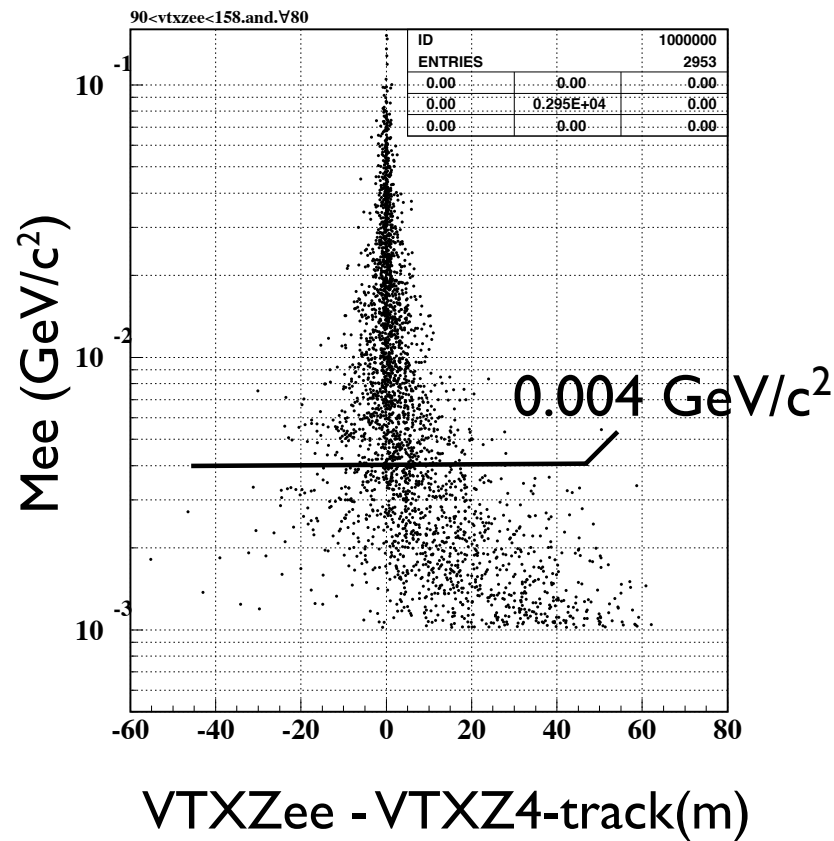


$\pi e$  tracks well agree with 4track vertex

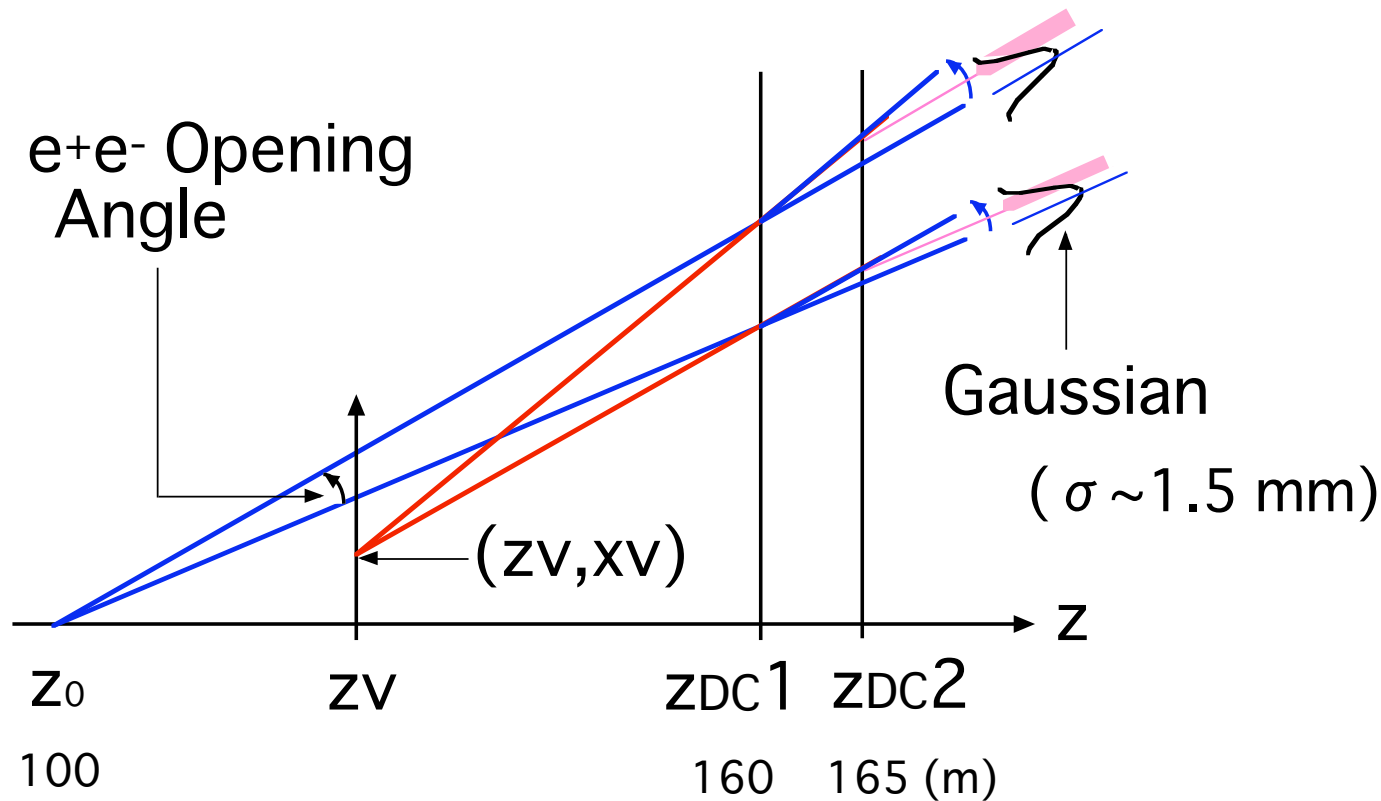


Some  $ee$  vertexZ are distributed in down stream.

# Small mass pairs stream downward well too.

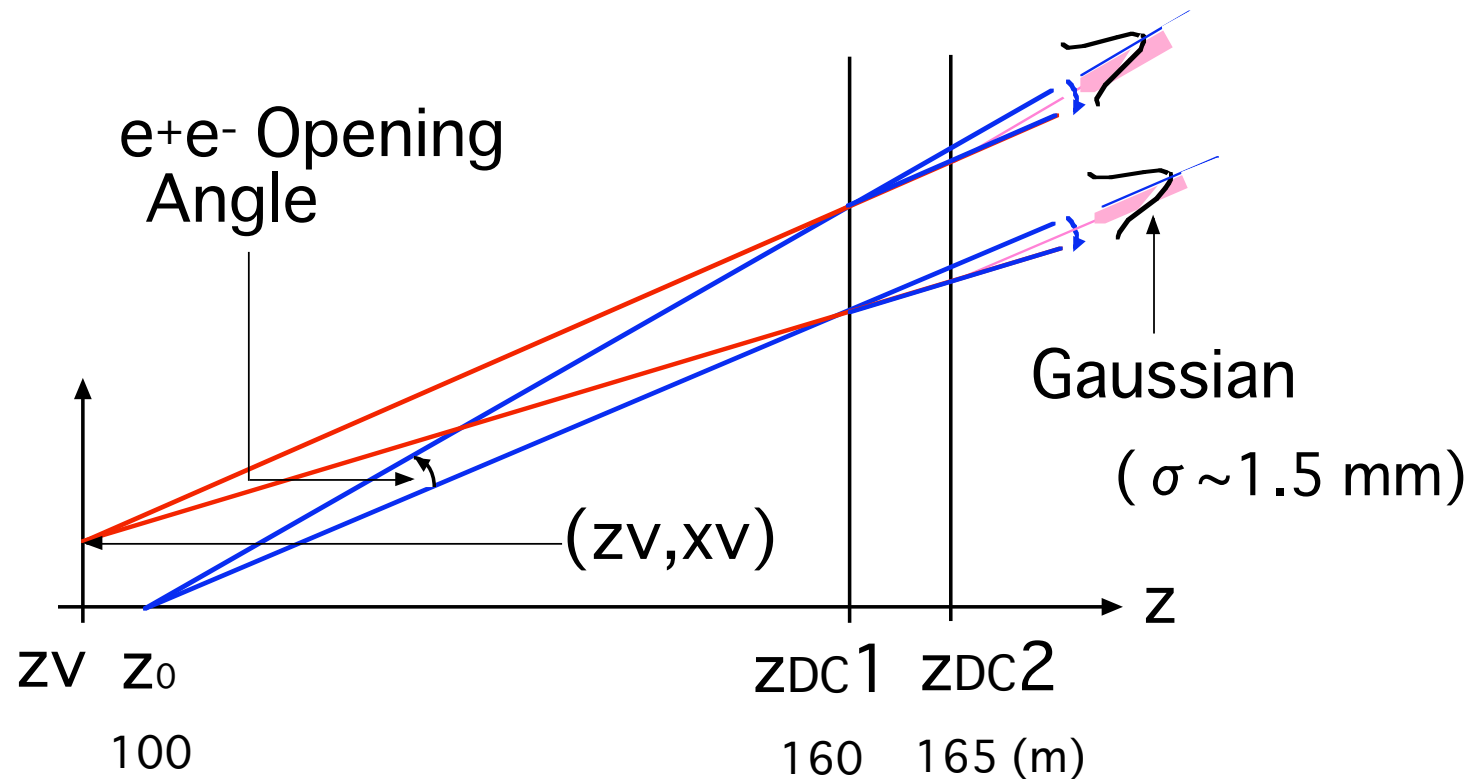


Between DC1 and DC2 an electron is scattered more than 1 mm at DC2



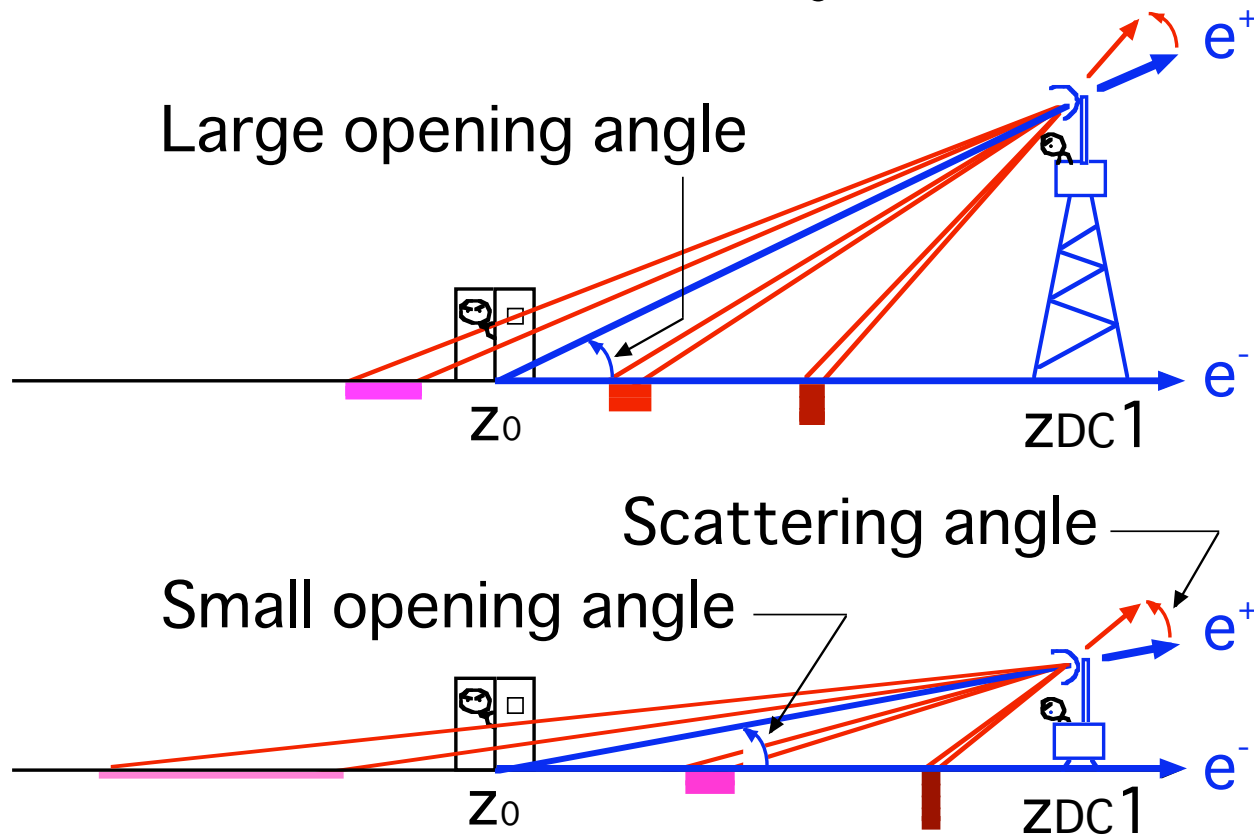
- Typical resolution of both DCs are  $100 \mu\text{m}$
- Integrated distribution of upper than  $Z_0$  and downer than  $Z_0$  must be same, but .....

Between DC1 and DC2 an electron is scattered more than 1 mm at DC2



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- Integrated distribution of upper than  $Z_0$  and downer than  $Z_0$  must be same, but ....

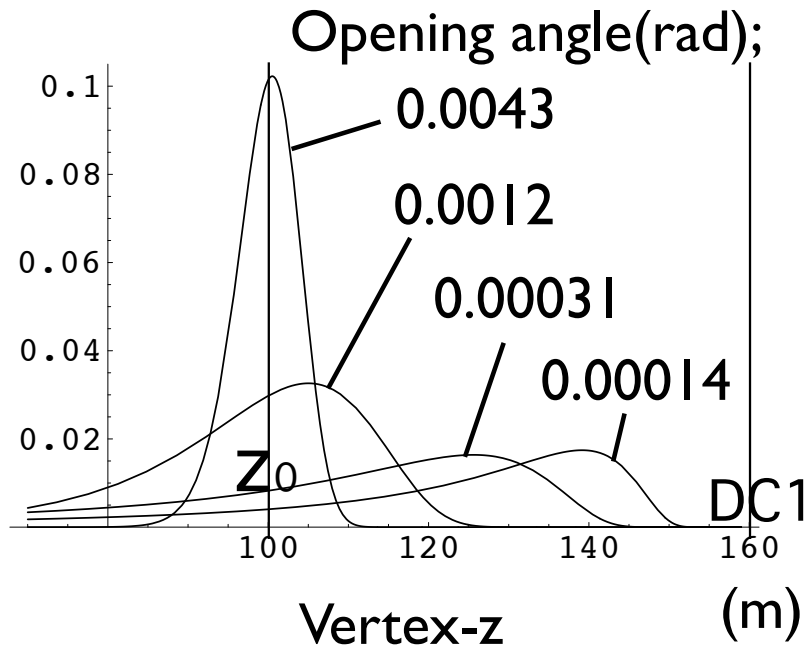
# You are a sentry of a jail house searching some jail breakers



- $e^+e^-$  opening angle at 4-track vertex is more sensitive than at  $e^+e^-$  pair track vertex.

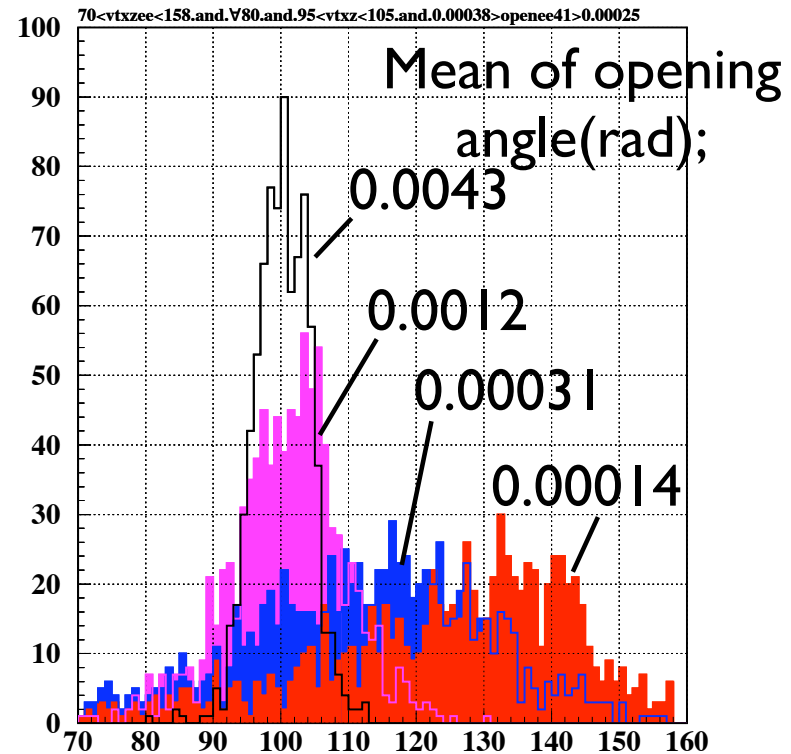
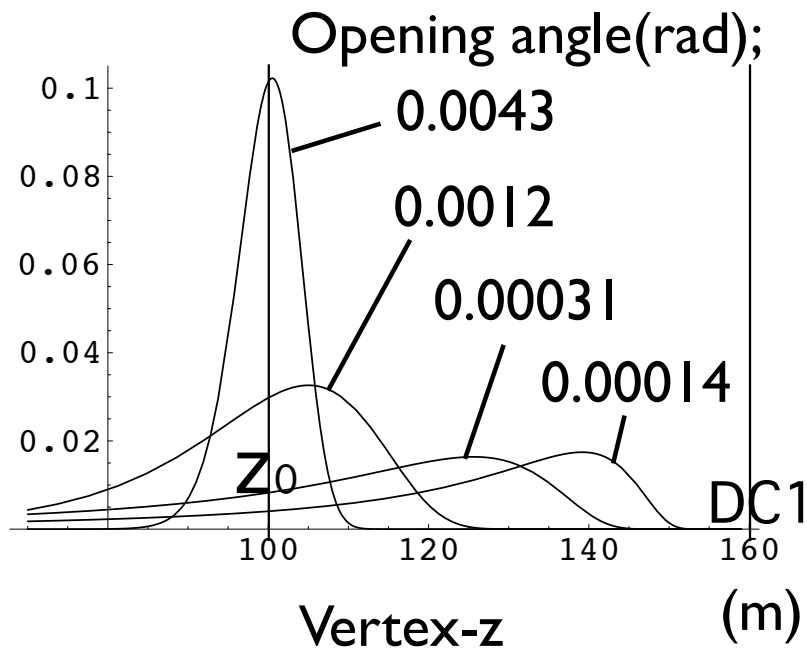


# Distribution of vertex-z depending on the opening angle



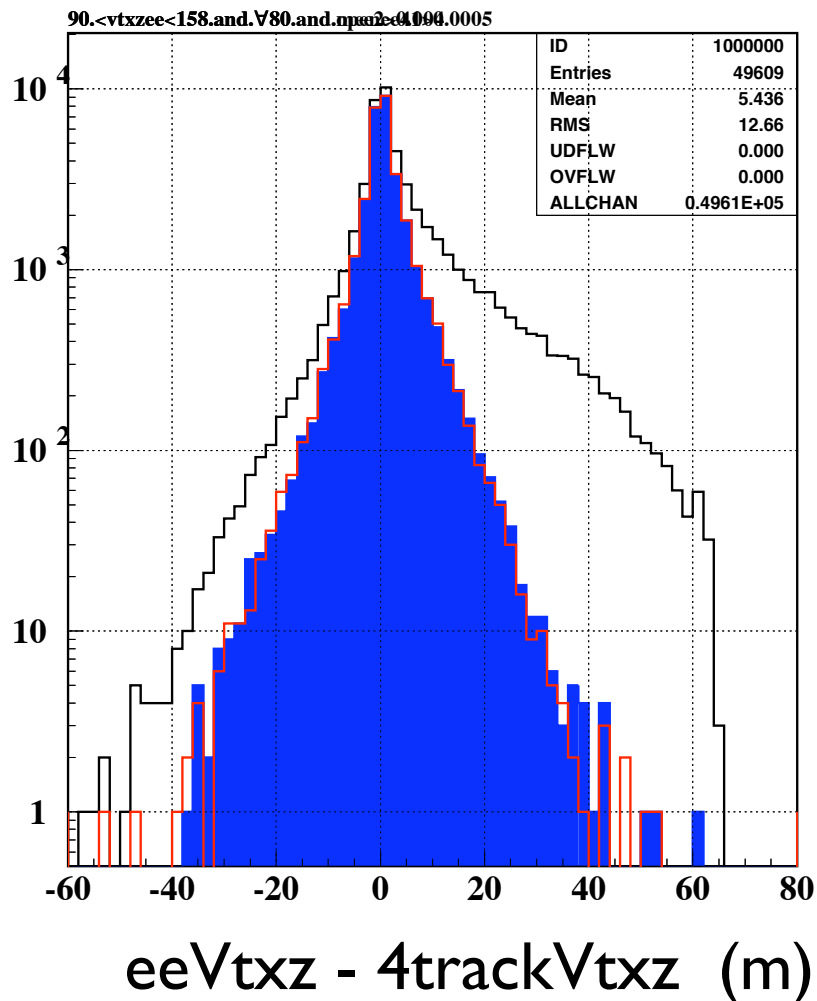
- Calculated distribution of vertex-z using previous model.
- Integrated area on the upper side of Z<sub>0</sub>(100 m) and the downer side are equal.

# Distribution of vertex-z depending on the opening angle



- Each hisotgram(right side) is vertex-z distribution of the events which has mean of opening angle same as calculated distributions(left side).

# Cut by invariantmass and opening angle of $e^+e^-$ pair



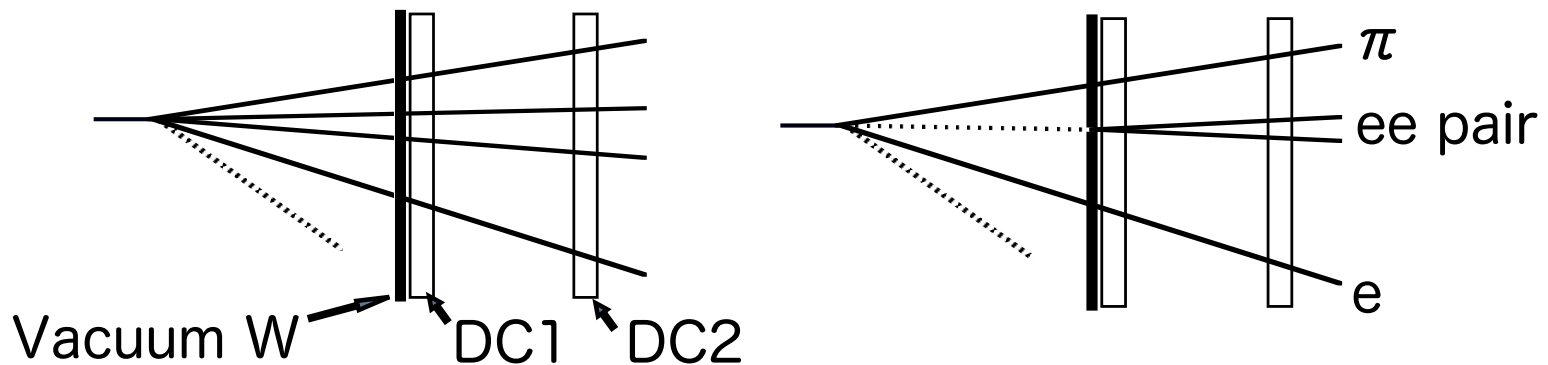
■  $e^+e^-$  opening angle  $>0.0005$ .

—  $M_{e^+e^-} > 0.004 \text{ GeV}/c^2$

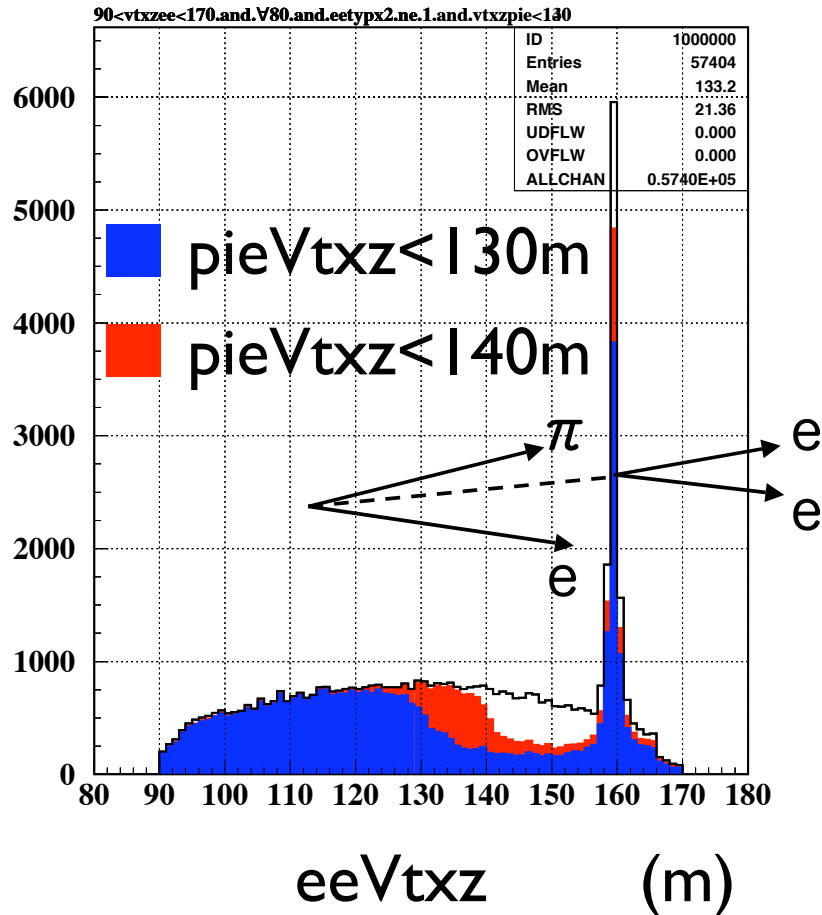
●  $M_{e^+e^-}^2 \sim E_{e^+}E_{e^-}\theta_{e^+e^-}^2$

# Separation of $K_L \rightarrow \pi e \nu ee$ and $K_L \rightarrow \pi e \nu \gamma$ with External Conv.

	$K_L \rightarrow \pi e \nu ee$	$K_L \rightarrow \pi e \nu \gamma$ with External Conv.
$\pi e$ -Vtx & $ee$ -Vtx	Agree	some distance
$ee$ -Vtx	not on Vacuum window	on Vacuum window



# How to remove 4-track Vtx event



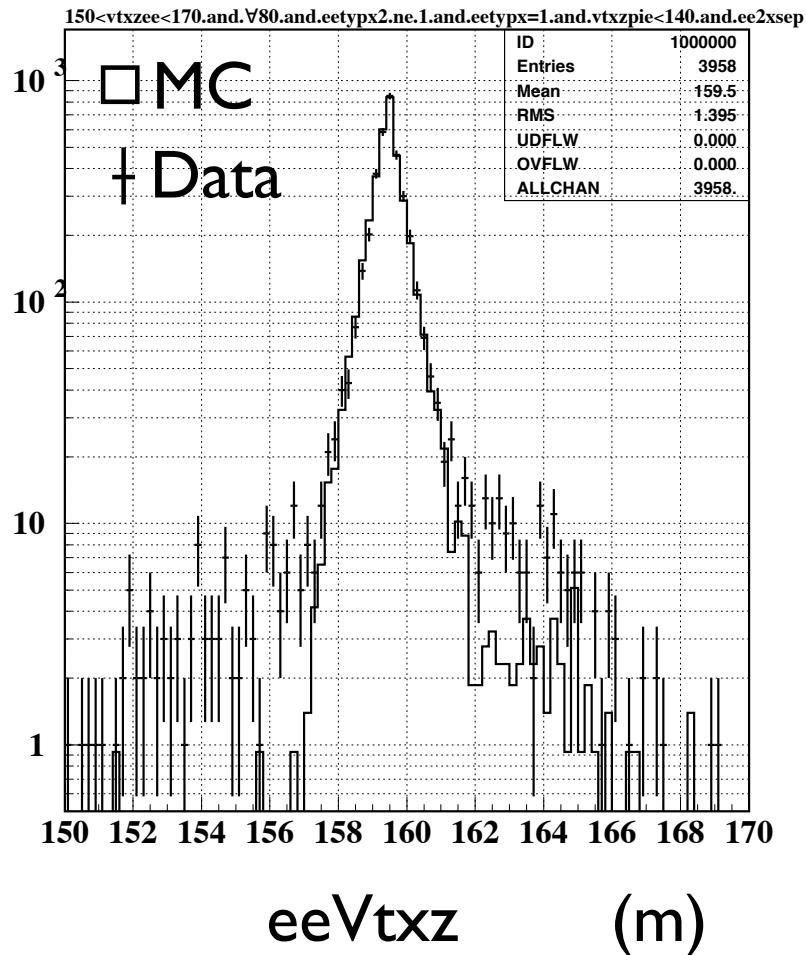
- This is not the real  $e^+e^-VtxZ$ , Because ...

- Separable distance in  $DCI > 0.001$  m

- Distance between  $DCI$  and  $DC2$  is 5 m

If Separation at  $DC2$  is  $0.0015$  m, event which has real  $eeVtxZ$  at 150 m can have  $eeVtxZ$  on  $DCI$  (Vacuum W).

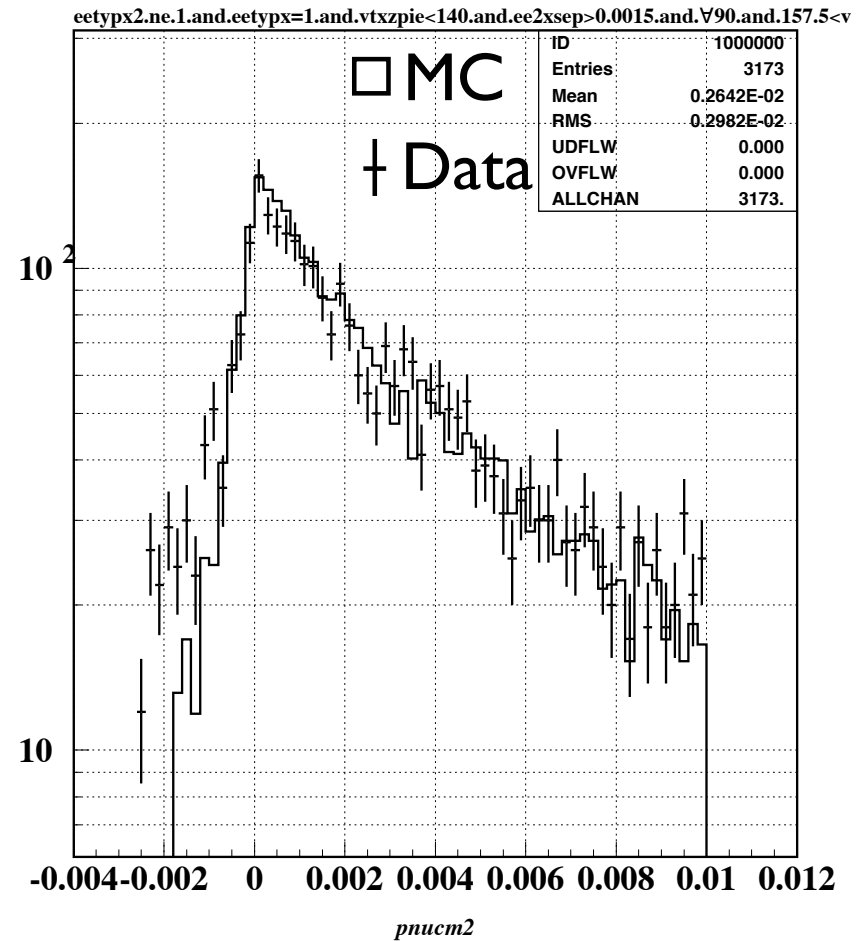
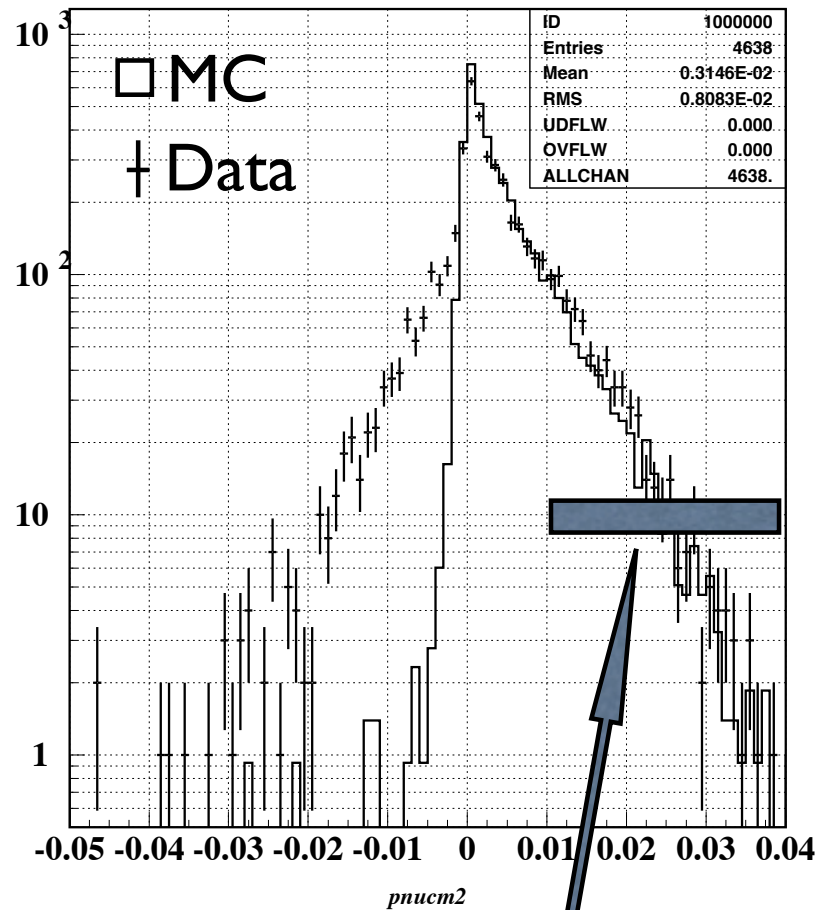
# Comparison with MC about eeVtxZ



- Separation at  $DC2 > 0.0015$  m
- Pie VtxZ < 140 m
- Real Vtx proj. on CSi must be Beam hole



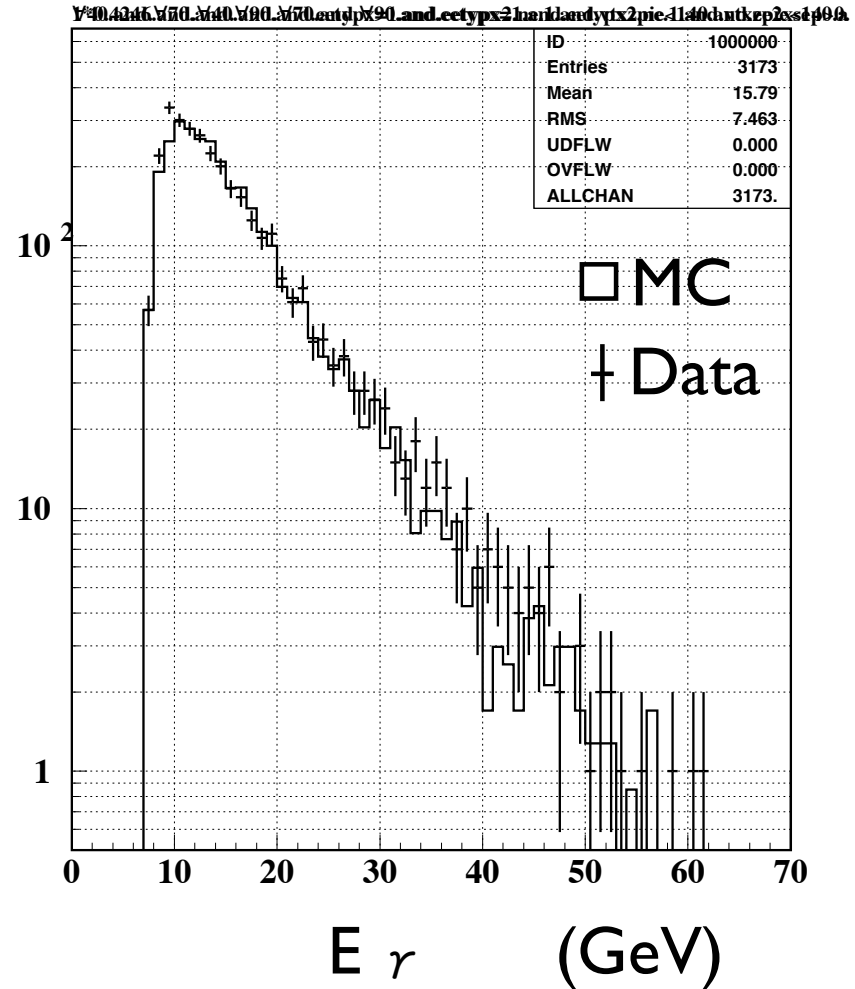
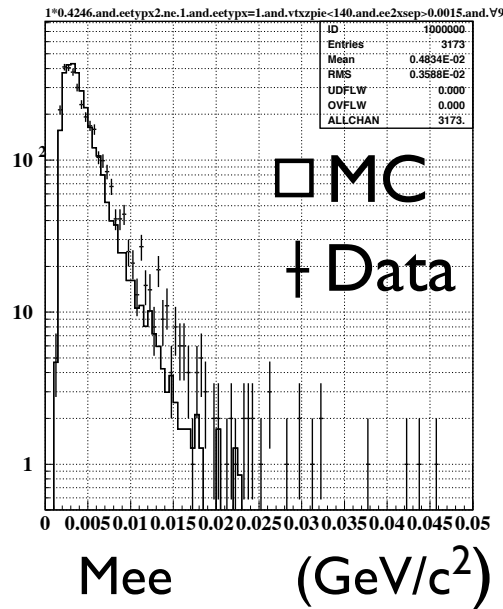
$$P_{\nu_{\parallel}} * 2$$



$\pi^+\pi^-\pi^0_{\text{Dal}}$  has a peak on this region.

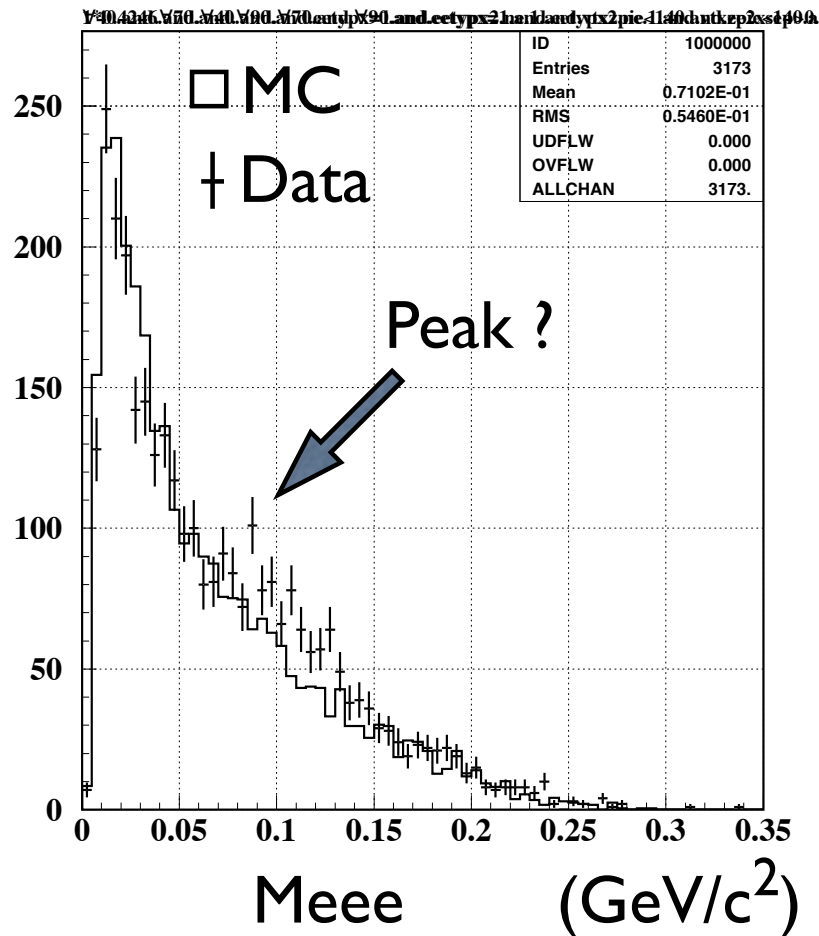


# Energy of reconstructed $\gamma$



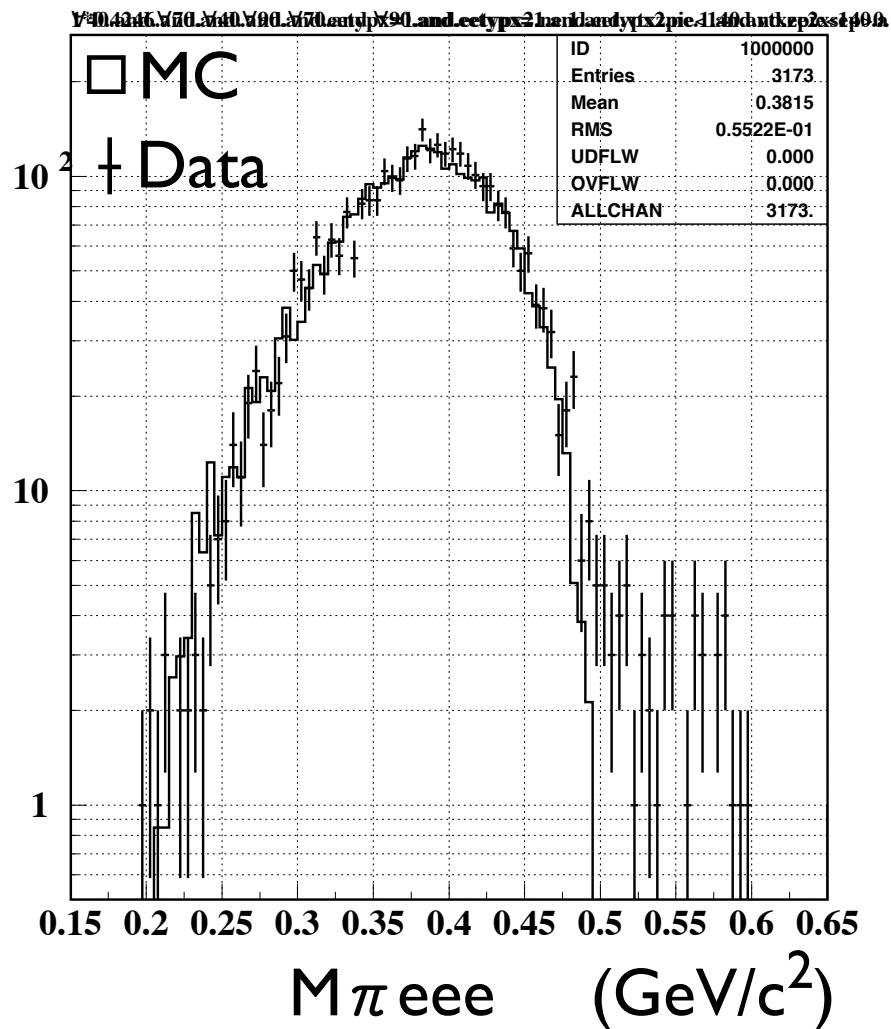
- Mee is very sensitive to manner of conversion

# Invariant mass of three electron



- There is a peak on 80~130 MeV
- They have no relation with large invariant mass of e e pair

# Invariant mass of $\pi eee$



- Agree with MC in smaller mass region than Kaon mass
- We can not use vertex  $\chi$  to remove unphysical invariant mass events

# Quantitative analysis of $K_L \rightarrow \pi e \nu \gamma$ with external conversion

- PDG requires that Energy of  $\gamma$  is greater than 30 MeV and Opening angle between electron and  $\gamma$  is greater than  $20^\circ$  in Kaon rest system
- Kaon momentum has ambiguity due to neutrino
- The way is comparison with MC
- Not yet ...

$$\text{Br}(K_{e3\gamma}:\text{free}??) = (7.93 \pm 0.17) \times 10^{-2} \text{ (only statistical error)}$$

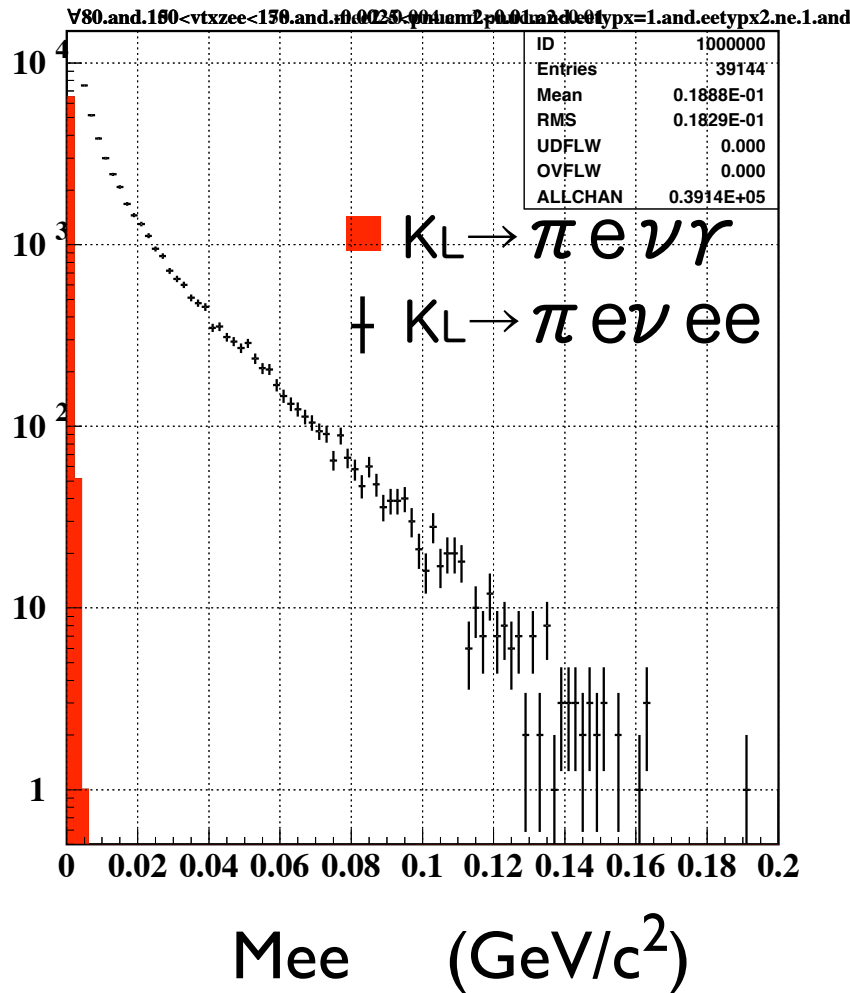
PDG;

$$\text{Br}(K_{e3\gamma}:E_\gamma^* > 30 \text{ MeV}, \theta_\gamma^* > 20^\circ) = (3.53 \pm 0.06) \times 10^{-3}$$

# Summary about $K_L \rightarrow \pi e \nu \gamma$ with external conversion

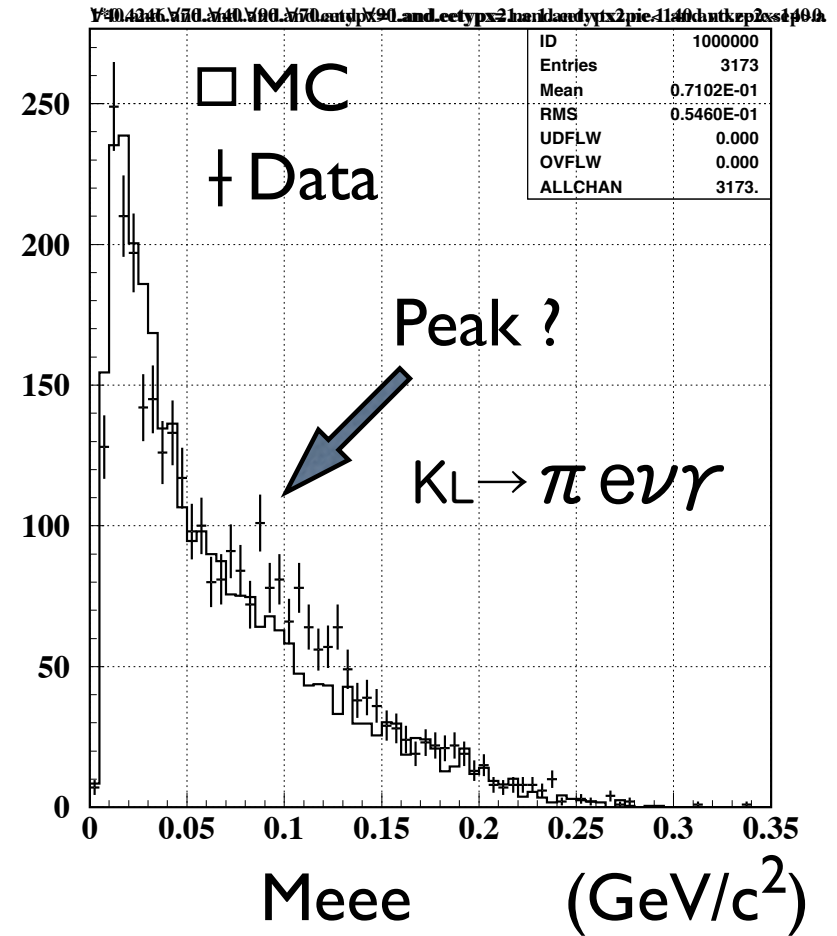
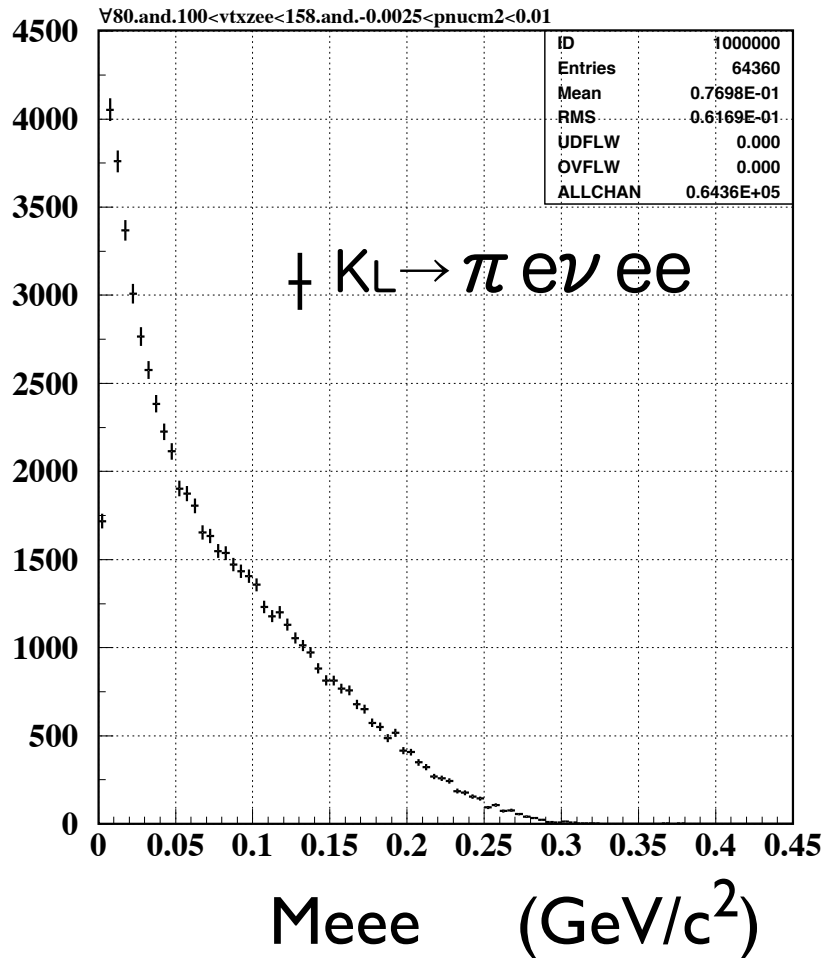
- Data has larger  $M_{ee}$  distribution than MC
  - Must be careful because  $M_{ee}$  is influenced by manner of conversion directly.
- Data has a peak at 80~130 MeV in the distribution of invariant mass of three electron
- I have to determine Kaon momentum in order to make the quantitative analysis.

# Invariant mass of ee pair comparing $K_L \rightarrow \pi e \nu \gamma$ and $K_L \rightarrow \pi e \nu ee$



- $K_L \rightarrow \pi e \nu ee$  has very large invariant mass of ee pair
- We have  $6 \times 10^4$   $K_L \rightarrow \pi e \nu ee$  candidates

# Invariant mass of three electron



# Summary

- Conclusion
  - I am trying to study Kaon structure using  $K_L \rightarrow \pi e \nu ee$  and radiative  $Ke3$  with external conversion
  - We can separate  $K_L \rightarrow \pi e \nu ee$  and  $Ke3 \gamma$  by relation of  $eeV_{tx}$  and  $\pi eV_{tex}$
  - We can see unknown peak in  $M_{eee}$  distribution
  - We have  $(4\sim 6) \times 10^4$  events of  $K_L \rightarrow \pi e \nu ee$  candidates
- Plan
  - Back ground estimation more rigorous
  - Must determine Kaon 4-momentum
  - MC for  $K_L \rightarrow \pi e \nu ee$